

## It is possible to assess the dynamic dependability of mechanical additives using comparable electricity usage. The Decline's Paths

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### Abstract:

*In mechanical systems, determining the precise direction of energy loss is very challenging. False reliability estimations may also be caused by ignoring the connection between residual energy at each load application along an electrical deterioration route. A dynamic reliability model for mechanical additives, which is defined by the distribution of material attributes and load in this work, may be used to address these issues. The models offered may be used to analyse statistical fabric qualities, such as failure rate and dependability. For a successful launch of a spacecraft, consultants may employ samples of explosive bolts to verify that their designs are both possible and accurate. Large mistakes in estimating dependability have also been identified when energy distribution software is used at each load. Both the dynamic dependability and mechanical additive failure rate of a material are controlled by its particular properties. part-to-part correlation and dynamic dependability of mechanical parts*

### INTRODUCTION

There must be a safety margin built in to mechanical components so that they can withstand environmental and material changes. They rely on their experience and industry expertise to ensure mechanical components are safe. Empirical safety factors do not account for mechanical design uncertainty and risk. As a consequence of this expansion, mechanical product reliability analysis has expanded [1–3]. That which can perform its intended functions without interruption for an extended period of time is referred to as a analysis. Traditional LSI models employ models with a fixed level of stability. There are several reasons that contribute to mechanical components breaking down over time in real-world applications. Further research on generalised approaches for mechanical component dynamic reliability analysis, according to Martin Traditional LSI models have their limits, and stochastic process theory reliability possible remedy. Two stochastic procedures are used to deal with the load and strength. It's one out of two; LSI and Markov models for time-dependent behaviour were used by Lewis[5] to study G redundant systems. Geidl and Saunders[6] used time-dependent elements in the reliability equation to quantify dependability. Using the generalised formula proposed by Somasundaram and Dhas[7], a dynamic parallel system in which the load is uniformly distributed may be evaluated. To ensure degradation processes are assumed to be continuous in time-dependent models employing stochastic process theory. While these reliability models may be

reliability, Noortwijk and Weide [8] developed a model that accounts for both load and strength. [9] Dynamic platform dependability was developed by the laboratory and its collaborators. Zhang et al. [10] employed Monte Carlo simulations and dynamic event trees [10] to calculate the dynamic dependability of nuclear power plants. Cutting tools and material flow were part of his research, as was industrial capacity. [12] A statistical process planning model developed by Barkallah and his colleagues was used to calculate production margins. These models include stochastic process models such as Markov and time-dependent models. The dynamic dependability of electronic components and multi-state systems may be studied using Markov models. The dynamic dependability of a model is evaluated using state transition matrices based on the changing states of components and systems across time using Markov models. In contrast, it is very difficult to precisely characterise and diagnose mechanical components. When external forces are applied to mechanical components, their structural integrity is compromised. Due to the absence of stress and material quality factors in state-based reliability models, mechanical components cannot be further examined. Dynamic reliability analysis of time-dependent models has also gotten a lot of attention in the last several years. Stress and strength used to dynamic reliability analysis for mechanical components that fail due to fatigue, there are numerous limitations. A discontinuous treatment is

used to mechanical components that have been exposed to wear and tear due to fatigue. There's no use in trying to figure out how reliable anything is at any one moment here. For further details, please see Section 1. At a certain period and amount of stress, a dynamic reliability study must be conducted. Dependability models that change over time based on load application intervals are simpler to develop than time-based models, for example. Reliability models based on load and strength losses are seldom employed in this context. The deterioration of strength in time-dependent models is simulated using stochastic processes without additional explanation of the physical meaning of parameters involved in the strength processes, for the purpose of efficiency. However, it is impossible to investigate the influence of statistical factors on reliability in these suggested dynamic reliability models. To determine how strength declines, it is challenging since the amount of force applied varies from time to time. As a result, reliability estimates are constantly reliant on the strength distribution at any given time or load application. " Reliability calculations may include large errors if the relationship between residual strength and each load application isn't taken into consideration. Including this in the present literature might result in inaccurate results. These problems may be addressed using dynamic reliability models that take mechanical component deterioration into account and that can be used to analyse statistical variations in material characteristics quantitatively. Stress, strength, and load application periods in the suggested models all include a random component. The suggested dependability models are not based on the distribution of strength, but rather on the strength degradation route.

The dependability models for random loads and their application periods are the subject of this section.

Consequently, the load process is distinct from corrosion failure mode when fatigue failure mode is just taken into account. An infinitesimal time period  $t$  has an infinite number of occurrences of load application because of the assumption that statistical properties of load are time-dependent. In this regard, the duration and amplitude of the imposed load should be considered major factors. As can be seen in Fig. 1, the strength does not decrease with time as

may be expected from a nonlinear failure mechanism.

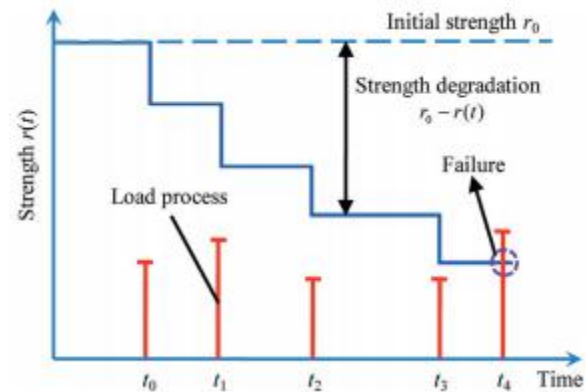


Figure 1 depicts a loss of power.

It is obvious from Figure 1 that the components' reliability equals one at any given time between two load applications, which is distinct from the reliability at any given time interval. Mechanical components with a fatigue failure mode cannot benefit from reliability tests conducted at a certain point in time. Because it is simpler and easier to understand, the relationship between strength and load application intervals is preferable to that of time. It is still uncommon to come across dynamic reliability models that take into account the deterioration of strength with time and the number of times that a load has been applied. Here, mechanical component dynamic reliability models are developed as a foundation for time-based dynamic reliability analysis. Additional considerations are made to determine how load and material factors affect reliability and failure rate.

Reliability models and the time it takes to load the software Strength deterioration is difficult to estimate since the amount of stress applied to each application varies widely. A stochastic process of strength degradation is employed in combination with the strength distribution at each load application to assess dynamic reliability. Some implausible deterioration trajectories for strength may be found in reliability estimates that take into consideration the strength distribution at each load application. In Fig. 2, you can see a variety of different deterioration trajectories. The random distribution of load magnitudes in each load application contributes to the uncertainty in the rate of strength degradation. The centre of Fig. 2 shows a potential change in strength when a load is applied to the material. As a result, the route of weakening may be described by changing points. Table 1 summarises all of the pathways shown in Fig. 2.

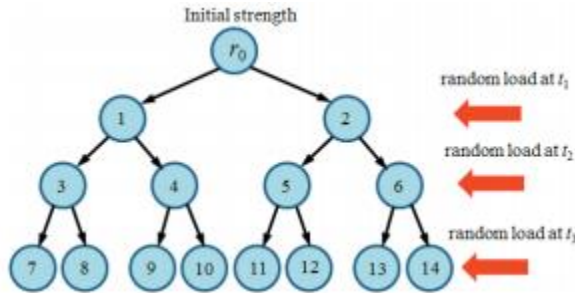


Fig. 2. Strength degradation path

Table 1. Strength degradation path

Strength degradation path	Changing point		
	$t_1$	$t_2$	$t_3$
$r_0-1-3-7$	1	3	7
$r_0-1-3-8$	1	3	8
$r_0-1-4-9$	1	4	9
$r_0-1-4-10$	1	4	10
$r_0-2-5-11$	2	5	11
$r_0-2-5-12$	2	5	12
$r_0-2-6-13$	2	6	13
$r_0-2-6-14$	2	6	14

On the first three time points, we see that there are two, four, and eight different places where strength may be altered (see Table 1). Including unlikely pathways like  $r_0-1-6-10$  and  $r_0-2-4-12$  in the strength distribution is taken into account when determining the dependability of each load application. As a result, a system's dependability might be misconstrued depending on the strength distribution at various load applications. Monte Carlo simulation may be used for dynamic reliability analysis. Based on their probability distributions, random loads are created and a deterioration process for mechanical components is simulated using this technique. Monte Carlo simulations take longer to execute as load application times grow. This has minimal practical use for the Monte Carlo simulation. The statistical aspects of material parameters on the dependability and failure rate of mechanical components cannot be adequately analysed using Monte Carlo simulation. In this part, we created dynamic reliability models that may be used to quantify mechanical component dependability under random load application over varied lengths of time. It is well-known how a thing loses strength. To sum up, the remaining mechanical components have a total strength of

$$r(n) = r_0 [1 - D(n)]^a, \quad (1)$$

$A$  is the material parameter, while  $n$  and  $a$  are the time and beginning strength values, respectively. There are two factors that define  $D(n)$ : the number of times a load is applied and its magnitude. In accordance with the Miner linear damage accumulation rule [14], a load with a magnitude of one causes:

$$D_i(n_i) = \frac{1}{N_i}, \quad (2)$$

Simultaneously, the component's life expectancy is measured in terms of  $N_i$ . the harm a load of magnitude  $s_0$  may do once is:

$$D_0(1) = 1 / N_0, \quad (3)$$

Under the load of  $s_0$ , the lifespan of a component is defined as  $N_0$ . A component's connection to load  $s_i$  and associated lifespan  $N_i$  may be represented mathematically using the S-N Curve theory, which states that the relationship is as follows:

$$s_i^m N_i = C, \quad (4)$$

Dispersion of the parameter  $C$  represents the dispersion of longevity. In the same way, the connection between and  $N_0$  may be expressed as follows:

$$s_0^m N_0 = C. \quad (5)$$

From Eq. (4) and Eq. (5), it can be derived that:

$$D_i(1) = \frac{1}{N_i} = \frac{s_i^m}{C}, \quad (6)$$

And

$$D_0(1) = \frac{1}{N_0} = \frac{s_0^m}{C}. \quad (7)$$

From Equation (6), it can be deduced that a load of magnitude  $s_i$  once results in the same damage as that produced by the same load of magnitude  $s_i$  for  $n_i 0$  times.

$$n_{i0} = \left(\frac{s_i}{s_0}\right)^m. \quad (8)$$

If a random load with a  $f(s)$  probability density function (pdf) is applied once, the damage it causes

may be approximated by the damage produced by the same load applied  $n_0$  times, according to the total probability theorem.

$$n_0 = \frac{1}{s_0^m} \int_{-\infty}^{\infty} s^m f_s(s) ds. \quad (9)$$

The remaining strength along an analogous strength degradation route may thus be defined as follows according to Eq. (1) for a deterministic starting strength:

$$\begin{aligned} r(n) &= r_0 [1 - D(n)]^n = r_0 \left(1 - \frac{n_0 n}{N_0}\right)^n = \\ &= r_0 \left(1 - \frac{n \int_{-\infty}^{\infty} s^m f_s(s) ds}{C}\right)^n. \end{aligned} \quad (10)$$

Given an initial strength  $R_0$  and a material parameter  $C$ , the component's reliability under  $n$  random loads may be calculated as follows:

$$R(n) = \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{C}\right)^r f_s(s) ds \right]. \quad (11)$$

Our starting strength and material parameter  $C$  are referred to as  $f_C$  and  $f_{r_0}$ , respectively, in order to represent their unpredictability. Reliability with regard to load application times and strength degradation may be described as follows using Bayes' rule for continuous variables:

$$R(n) = \int_{-\infty}^{\infty} f_{r_0}(r_0) \int_{-\infty}^{\infty} f_C(C) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{C}\right)^r f_s(s) ds \right] \right\} dC dr_0. \quad (12)$$

The failure rate of components with regard to load application periods may be stated as follows according to the definition of failure rate:

$$\begin{aligned} h(n) &= \frac{F(n+1) - F(n)}{R(n)} = \\ &= \left\{ \int_{-\infty}^{\infty} f_{r_0}(r_0) \int_{-\infty}^{\infty} f_C(C) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{C}\right)^r f_s(s) ds \right] \right\} dC dr_0 - \right. \\ &\quad \left. - \int_{-\infty}^{\infty} f_{r_0}(r_0) \int_{-\infty}^{\infty} f_C(C) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{C}\right)^r f_s(s) ds \right] \right\} dC dr_0 \right\} / \\ &\quad \left\{ \int_{-\infty}^{\infty} f_{r_0}(r_0) \int_{-\infty}^{\infty} f_C(C) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{C}\right)^r f_s(s) ds \right] \right\} dC dr_0 \right\}. \end{aligned} \quad (13)$$

This equation degenerates into the following form in the absence of strength degradation:

$$R(n) = \int_{-\infty}^{\infty} f_{r_0}(r_0) \left[ \int_{-\infty}^{\infty} f_s(s) ds \right]^n dr_0. \quad (14)$$

When  $n$  is equal to 1, Eq. (14) may be simplified to the standard LSI model.

This section uses experiments with explosives to demonstrate the suggested reliability models. Explosive bolts are required for successful satellite launches as a pyrotechnic attachment and separation mechanism. Figure 3 [15] depicts the explosive bolt's structure. An explosive bolt is used to connect the payload adapter to the satellite's interface ring. It is possible to break an explosive bolt with the use of a power source provided by an explosive charge during the departure procedure for satellites and launch vehicles. Satellite failure might occur if the bolt's strength decreases during launch. Dynamic dependability of explosive bolts that are utilised for satellite launches will be examined here.

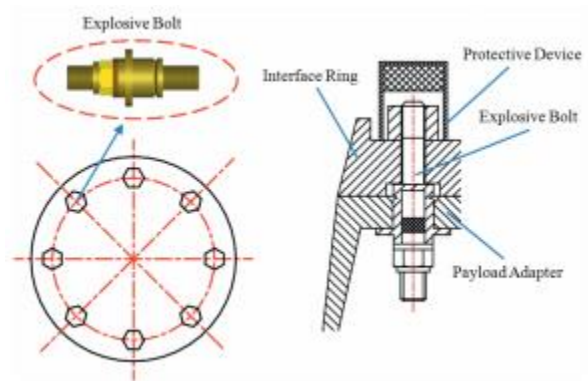


Figure 3 shows the explosive bolt's structure.

There is a considerable degree of uncertainty in the ambient load during satellite launch, and this uncertainty is increased by the manufacturing process

of explosive bolts." Mechanical components are employed to endure shear pressures, whilst explosive bolts are utilised to launch satellites [11]. [10, 12]. Figure 4 demonstrates how a finite element analysis (FEA) may be used to determine the distribution of explosive bolt stress. Experiments may be conducted to determine the distribution of initial strength. Please refer to [16] for additional information on constructing a finite element model of bolted joints. Crocombe[17] also created an energy estimate approach. In order to analyse the behaviour of stainless steel linked connections, Nethercot employed finite element models. According to Oskouei [19], he utilised the finite-element technique to investigate an aircraft structural double-lapbolted joint. When threaded fasteners spin in contact with one other, Nassar's technique may be used to compute the frictional forces that arise. Explosive bolts are put to the test in this study to discover how differences in material factors impact their overall dependability and failure rate.

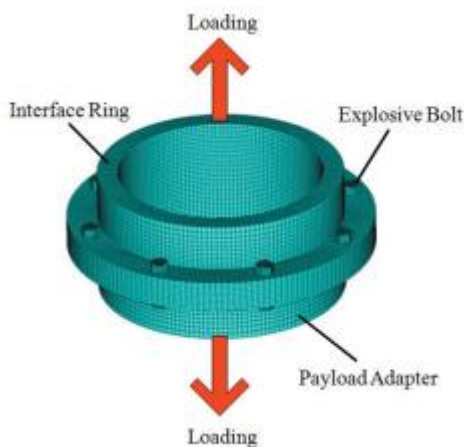


Fig. 4 depicts a finite element model of a blasting device.

The two parameters for the explosive bolts are  $m = 2$ ,  $n = 1$ , and  $C = 109 \text{ MPa}^2$  for the material. The normal distribution is used to characterise the initial explosive bolt strength ( $r_0$ ) and its standard deviation ( $\sigma(r_0)$ ). Each time a certain load is applied, a normal distribution with an average value of  $\mu(s)$  and a standard deviation of  $\sigma(s)$  is observed. Using Table 2, you can see the average and standard deviation of the initial strength and stress levels.

Table 2 shows the results for stress and starting strength.

$\mu(r_0)$ [MPa]	$\sigma(r_0)$ [MPa]	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]
600	20	500	20

In order to verify the accuracy of the reliability model presented in Section 1.1, we run a Monte Carlo simulation to test the explosive bolts' dynamic dependability. The flowchart for the Monte Carlo simulation may be seen in Figure 5. A Monte Carlo simulation is used to model the strength degradation of an explosive bolt sample in relation to the degradation process and the stress created throughout the strength degradation pathway. Bolt strength loss may be accurately modelled using Monte Carlo simulation. Equation may also be used to determine the strength distribution for each load application (10). Figure 6 displays probable errors in the reliability calculation, showing how these elements combine to cause biases, based on a Monte Carlo simulation and the strength distribution for each load application.

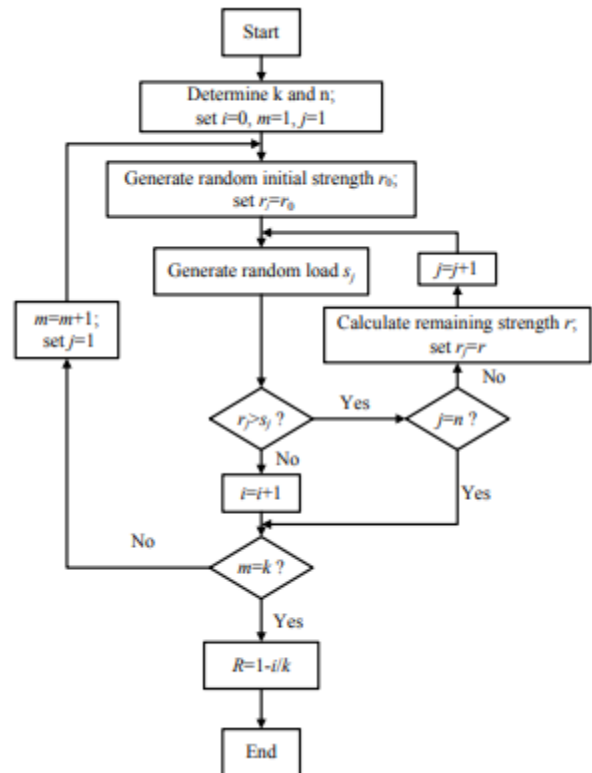


Fig. 5. Flowchart of Monte Carlo simulation

In Fig. 6, we can clearly see that the proposed method's reliability estimates are in great agreement with Monte Carlo simulation results. Reliability may be incorrectly calculated if the distribution of strength at each load application does not take into account any possible channels of deterioration, and instead takes into account just those that are known to exist.

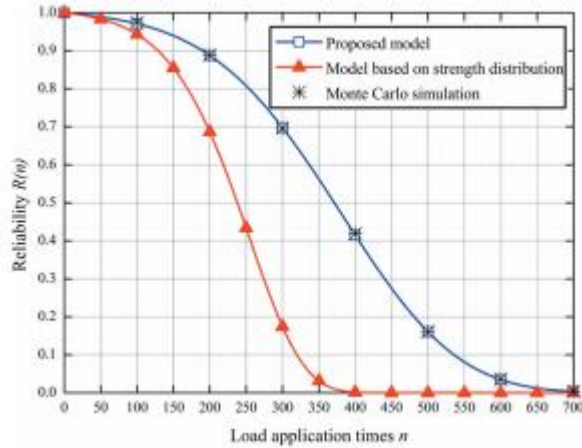


Figure 6 illustrates the Monte Carlo simulation against the proposed method.

Explosive bolts' reliability and failure rate may be better understood by examining the following four situations.  $m = 2$  and  $r_0 = 600$  MPa are the characteristics of the explosive bolts in case 1. Table 3 gives the statistical characteristics for stress and C. Various mean values of C are used to test the explosive bolts' dependability and failure rates, which are shown in figures 7 and 8.

Explosive bolt C stress and material parameters C are summarised in Table 3.

	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]	$\mu(C)$ [MPa <sup>2</sup> ]	$\sigma(C)$ [MPa <sup>2</sup> ]
1	500	20	$10^9$	$10^6$
2	500	20	$1.5 \times 10^9$	$10^6$
3	500	20	$2 \times 10^9$	$10^6$

If  $m = 2$ ,  $\sigma = 1$ , and  $r_0$  is 600 MPa, then the material properties of the explosive bolts are as follows: Table 4 lists the statistical characteristics of stress and C. Figures 9 and 10 illustrate the dependability and failure rates of the explosive bolts with various standard deviations of C.

The fourth table. Explosive bolts' stress and material C characteristics, as measured statistically

	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]	$\mu(C)$ [MPa <sup>2</sup> ]	$\sigma(C)$ [MPa <sup>2</sup> ]
1	500	20	$10^9$	$10^6$
2	500	20	$10^9$	$5 \times 10^6$
3	500	20	$10^9$	$10^7$

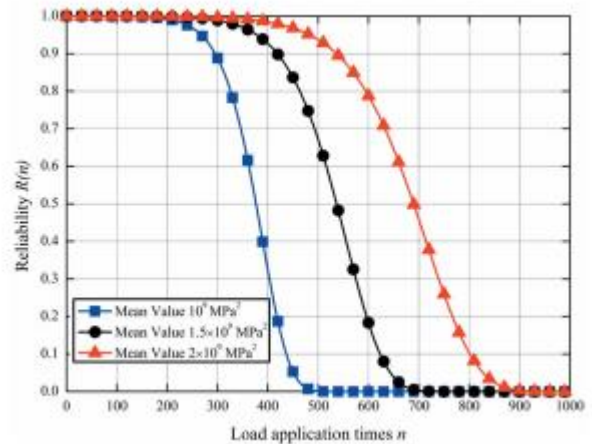


Fig. 7. Reliability of explosive bolts with different mean values of C

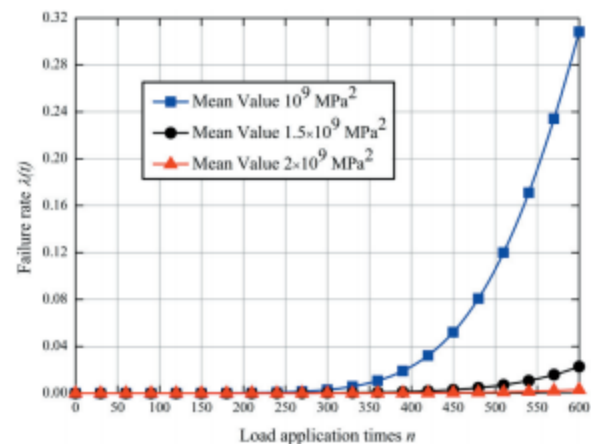


Fig. 8. Failure rate of explosive bolts with different mean values of C

At  $m=2$ ,  $\sigma=1$  and  $C=109$  MPa<sup>2</sup> are provided as the material properties of the explosive bolts. Table 5 presents the statistical data for both stress and beginning strength. Figures 11 and 12 illustrate the dependability and failure rate of the explosive bolts with varying mean beginning strengths.

Data on stress and initial strength of explosive bolts are shown in Table 5.

	$\mu(r_0)$ [MPa]	$\sigma(r_0)$ [MPa]	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]
1	550	30	500	20
2	600	30	500	20
3	650	30	500	20

Assume that  $m = 2$ ,  $\sigma = 1$ , and  $C=109$  MPa<sup>2</sup> are the material characteristics of the explosive bolts. Table

6 summarises the statistical data on stress and beginning strength. Reliability and failure rate

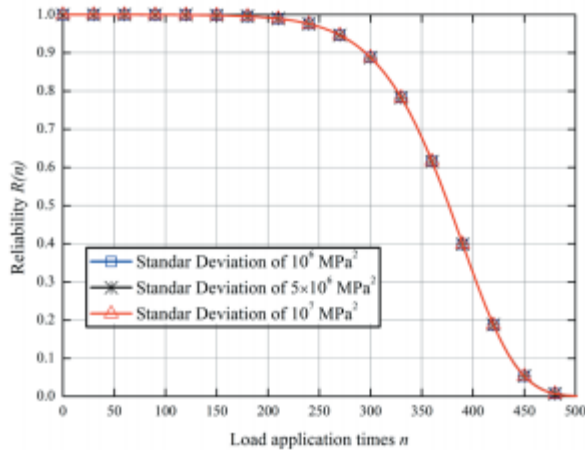
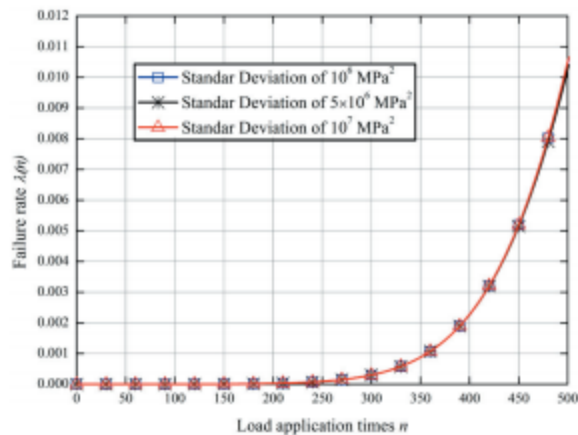


Fig. 9. Reliability of explosive bolts with different dispersions of C



Figures 13 and 14 demonstrate the failure rate of explosive bolts with various dispersions of the C rate of the explosive bolts with different standard deviations of starting strength.

Data on stress and initial strength of explosive bolts are shown in Table 6.

	$\mu(r_0)$ [MPa]	$\sigma(r_0)$ [MPa]	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]
1	600	20	500	20
2	600	30	500	20
3	600	40	500	20

Case 5: The explosive bolts' material characteristics are  $m=2$ ,  $=1$ , and  $C=109$  MPa<sup>2</sup>. Table 7 lists the stress and  $r_0$  statistical characteristics. Figure 15 depicts the explosive bolts' dependability under various stress dispersions.

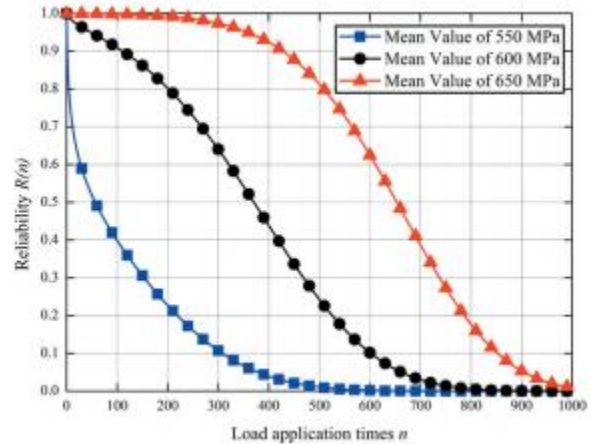


Fig. 11. Reliability of explosive bolts with different mean values of initial strength

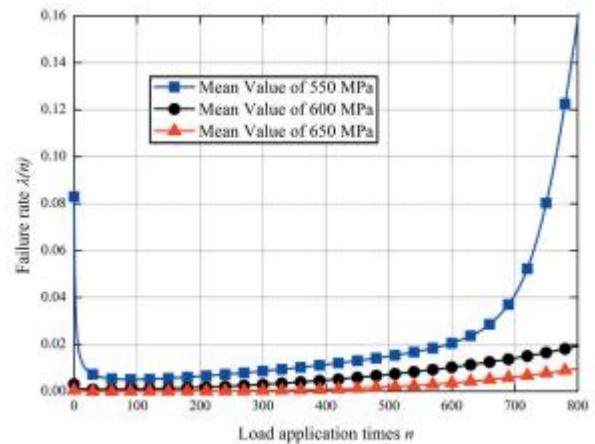


Fig. 12. Failure rate of explosive bolts with different mean values of initial strength

Table 7. Statistical parameters of stress and material parameters C of explosive bolts

	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]	$\mu(r_0)$ [MPa]	$\sigma(r_0)$ [MPa]
1	500	10	600	30
2	500	20	600	30
3	500	30	600	30

Figures 7 to 12 show that the dependability and failure rate of explosive bolts are strongly influenced by the mean starting strength and C. As the mean starting strength and C rise, so does the dependability, and the failure rate follows suit. Additional to this, C's spread does not affect the dependability or failure rate of explosive bolts, therefore it may be ignored in the examination of explosive bolts' failure rates. The following is a rewrite of Eqs. (12) and (13):

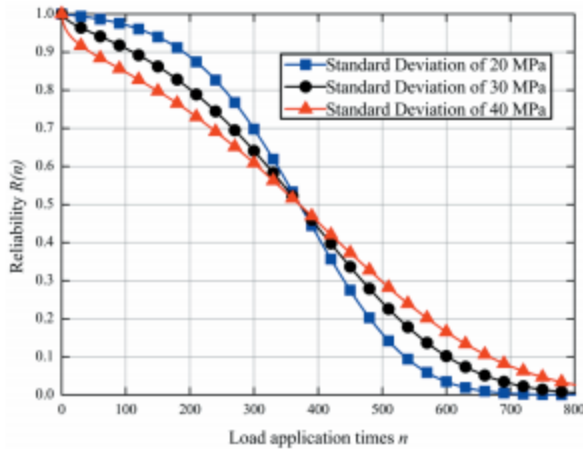


Fig. 13. Reliability of explosive bolts with different dispersions of initial strength

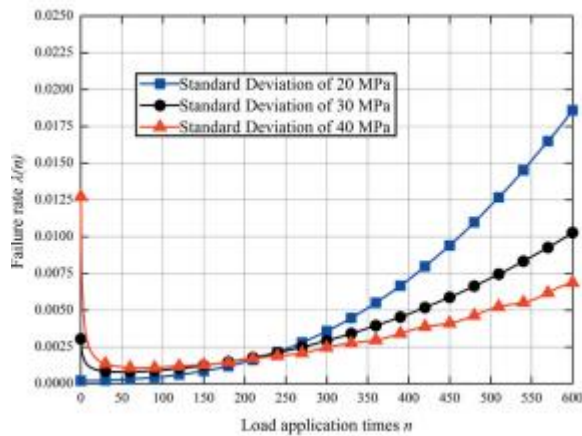


Fig. 14. Failure rate of explosive bolts with different dispersions of initial strength

$$R(n) = \int_{-\infty}^{\infty} f_0(r_0) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{c} \right)^r f_s(s) ds \right] \right\} dr_0,$$

$$h(n) = \left\{ \int_{-\infty}^{\infty} f_0(r_0) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{c} \right)^r f_s(s) ds \right] \right\} dr_0 - \right.$$

$$\left. - \int_{-\infty}^{\infty} f_0(r_0) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{c} \right)^r f_s(s) ds \right] \right\} dr \right\} /$$

$$/ \left\{ \int_{-\infty}^{\infty} f_0(r_0) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} \left(1 - \frac{\int_{-\infty}^{\infty} s^m f_s(s) ds}{c} \right)^r f_s(s) ds \right] \right\} dr_0 \right\}.$$

A big dispersion is also associated with decreased dependability, according to conventional wisdom. Figures 13 and 14 show that the dispersion of starting strength effects the dependability and failure rate of explosive bolts at various points in their lifespan. To put it another way, a significant dispersion in starting strength increases the likelihood that the remaining strength will have a low value, which results in poor dependability over the early period of life. A broad dispersion of starting strength improves the likelihood that the remaining strength has a significant value, which leads to a high level of dependability at the beginning of its existence.

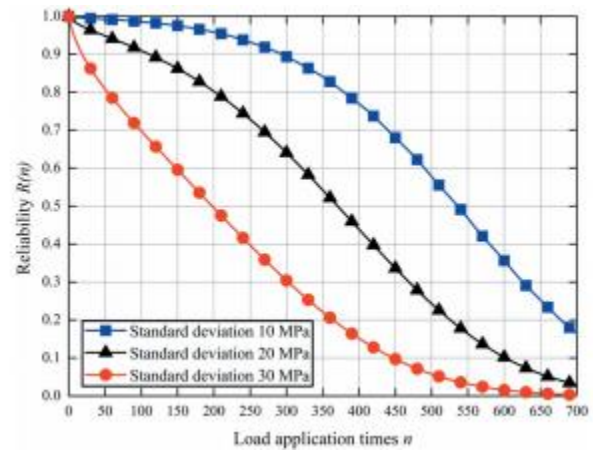


Figure 15 shows that the standard deviation of the dependability of explosive bolts under stress is shown to change with the stress.

The stress distribution has a significant impact on the dynamic dependability of explosive bolts, as shown in Fig. 15. Stress dispersion has a detrimental impact on system dependability. In other words, if the stress is distributed too widely during the load application process, it is more likely to surpass its residual strength.

### Dynamic Reliability Analysis of Mechanical Components

The failure mechanism and the stochastic strength degradation pathway have been taken into consideration in the development of dynamic reliability models for time. The dynamic dependability and failure rates of mechanical components are also examined using numerical examples of beginning strength statistics.

### Dynamic Reliability Models Consider Time as a Factor



Because mechanical components with fatigue failure modes cannot have continuous load statistics with reference to time, this implies, as previously noted, a limited number of load repetitions in an infinitesimal time period  $t$ . In order to accurately assess loading, it is necessary to consider both the amount of time and weight involved. Section 1.1 provides a framework for building time-based dependability models, so these models may be used. As load application periods are linked to time, the dynamic dependability of components with regard to time may be further enhanced. Calculating dynamic mechanical component dependability using the following equation is possible if load application times are known for an interval of that length.

$$R(t) = \int_{-\infty}^{\infty} f_r(r_0) \left\{ \prod_{i=0}^{f_r(t)-1} \left[ \int_{-\infty}^{\infty} r^{(1-\frac{i}{c})} f_s(s) ds \right]^c \right\} dr_0. \quad (15)$$

Nonetheless, stochastic process theory can only be used to analyse random load occurrences. Using the Poisson process to represent the random occurrence times of random load in an interval has been shown to be an effective stochastic process. There are  $n$  times that the random load will emerge during the specified period of time, according to the theory of the Poisson process [6].

$$\Pr[n(t) - n(0) = n] = \frac{(\int_0^t \lambda(t) dt)^n}{n!} \exp(-\int_0^t \lambda(t) dt), \quad (16)$$

where  $(t)$  is the Poisson process's intensity. A mechanical component's dependability over a time period of  $t$  may be described as follows using the total probability theorem for an initial strength of determination  $(r)$ :

$$\begin{aligned} R(t) &= \sum_{k=0}^{\infty} P(n(t) = k) R(k) = \\ &= \exp(-\int_0^t \lambda(t) dt) + \sum_{n=1}^{\infty} \frac{(\int_0^t \lambda(t) dt)^n}{n!} \times \\ &\times \exp(-\int_0^t \lambda(t) dt) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} r^{(1-\frac{i}{c})} f_s(s) ds \right]^c \right\}. \end{aligned}$$

When considering the distribution of initial strength characterised by its pdf of  $f_r(r)$ , the reliability can be obtained by using the Bayes law for continuous variables as follows:

$$\begin{aligned} R(t) &= \int_{-\infty}^{\infty} f_r(r) \exp(-\int_0^t \lambda(t) dt) + \sum_{n=1}^{\infty} \frac{(\int_0^t \lambda(t) dt)^n}{n!} \times \\ &\times \exp(-\int_0^t \lambda(t) dt) \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} r^{(1-\frac{i}{c})} f_s(s) ds \right]^c \right\} dr. \quad (17) \end{aligned}$$

Correspondingly, the failure rate of the component can be written as:

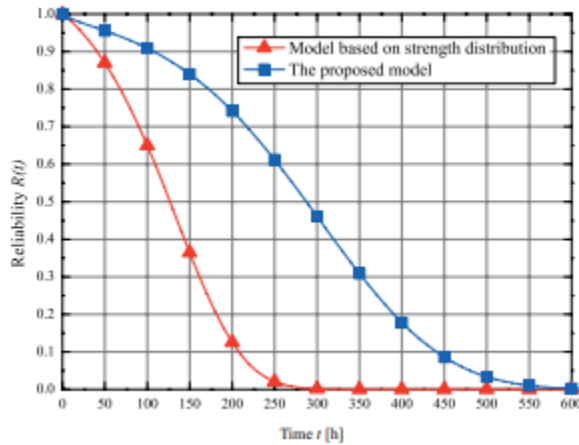
$$\begin{aligned} h(t) &= \left\{ \lambda(t) \int_{-\infty}^{\infty} f_r(r) \left[ 1 - \sum_{n=1}^{\infty} \frac{(\int_0^t \lambda(t) dt)^{n-1}}{n!} \left[ n - \int_0^t \lambda(t) dt \right] \times \right. \right. \\ &\times \left. \left. \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} r^{(1-\frac{i}{c})} f_s(s) ds \right]^c \right\} \right] \right\} / \\ &/ \left\{ \int_{-\infty}^{\infty} f_r(r) \left[ 1 + \sum_{n=1}^{\infty} \frac{(\int_0^t \lambda(t) dt)^n}{n!} \times \right. \right. \\ &\times \left. \left. \left\{ \prod_{i=0}^{n-1} \left[ \int_{-\infty}^{\infty} r^{(1-\frac{i}{c})} f_s(s) ds \right]^c \right\} \right] \right\} dr. \quad (18) \end{aligned}$$

However, the time-based reliability model in Section 2.1.1 is based on the theory of Poisson processes, but the model is readily adaptable to other dynamic models if the statistical properties of load application times are known. Eqs. 17 and 18 show that mechanical components' stochastic strength degradation trend is taken into account in the proposed dynamic reliability model. There will be an example of the inaccuracy of using each load application to determine reliability in the next section.

There are mathematical explanations of 2.2. Take into account the explosive bolts' random loads and Poisson-like occurrence times. Stress and starting strength are distributed in a typical manner. The explosive bolts have material characteristics of  $m = 2$ ,  $= 1$ , and  $C = 108 \text{ MPa}^2$ . Information on stress and starting strength is included in Table 8. As shown in Fig. 16, the system's dependability is shown in various conditions using the models proposed in this research and the distribution of strength in each load application.

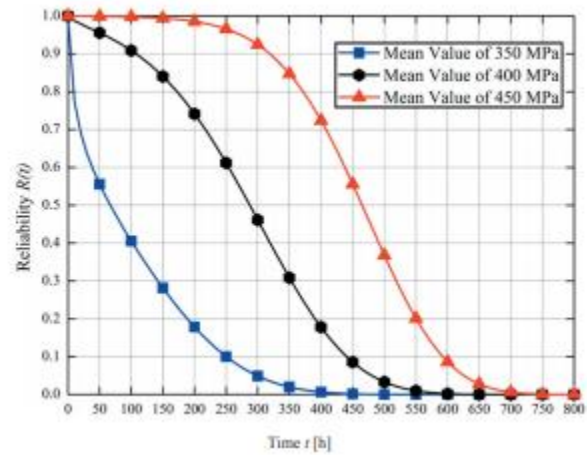
These experiments have given some intriguing findings.

$\mu(r_0)$ [MPa]	$\sigma(r_0)$ [MPa]	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]
400	30	300	20

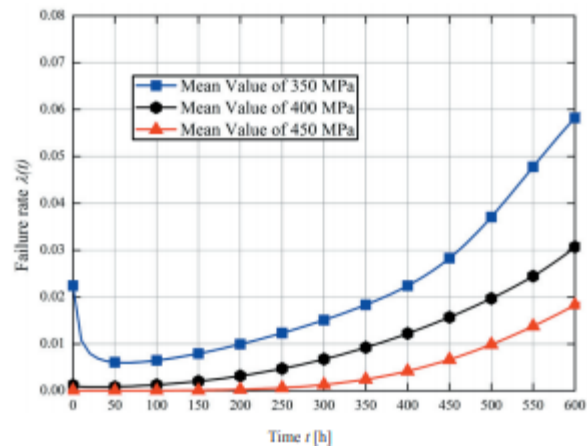


*The suggested method's reliability in contrast to that estimated using the strength distribution shown in Fig. 16.*

In Fig. 16, the recommended reliability models may be applied to depict how dependability evolves over time. Using a dispersion of strength at each load application diminishes the overall reliability of the system. The difficulty originates from the notion that strength degradation mechanisms that do not exist exist. Consider the strength degradation path rather than the amount of load delivered at any one moment when creating dynamic reliability models. Consider the following two circumstances to get a better grasp of how initial strength effects explosive bolt reliability and failure rates: If the explosive bolts have material characteristics  $m = 2$ ,  $\beta = 1$ , and  $C$  equal to  $108 \text{ MPa}^2$ , then this is the first scenario. Both stress and starting strength are evaluated in Table 9. Experiments with explosive bolts of different initial strength revealed similar results (Figures 17 and 18). (Figures 17 and 18).  $m=2$ ,  $\beta = 1$ , and  $C=108 \text{ MPa}^2$  are some examples of material specifications for the explosive bolts.



*Fig. 17. Reliability of explosive bolts with different mean values of initial strength*



*Figure 18 shows the failure rate of explosive bolts when the starting strength is varied by a mean.*

Table 10 displays the statistical properties of stress and beginning strength. Figures 19 and 20 illustrate the dependability and failure rate of explosive bolts with various standard deviations of starting strength.

Statistics of stress and initial strength in explosive bolts are summarised in Table 9.

	$\mu(r_0)$ [MPa]	$\sigma(r_0)$ [MPa]	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]
1	350	30	300	20
2	400	30	300	20
3	450	30	300	20

As shown in Figs. 17 to 20, the suggested dynamic reliability models may be utilised to analyse the dynamic features of reliability as well as quantitatively analyse the effect of environmental conditions on reliability and failure rate, as shown

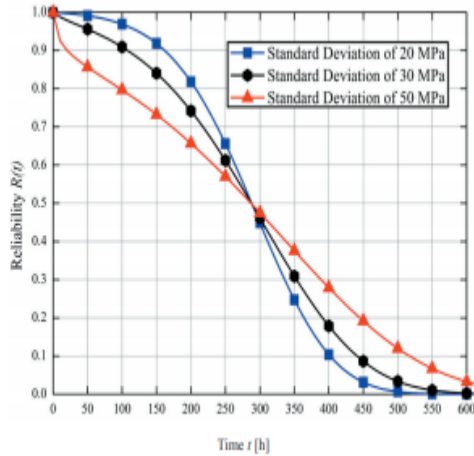
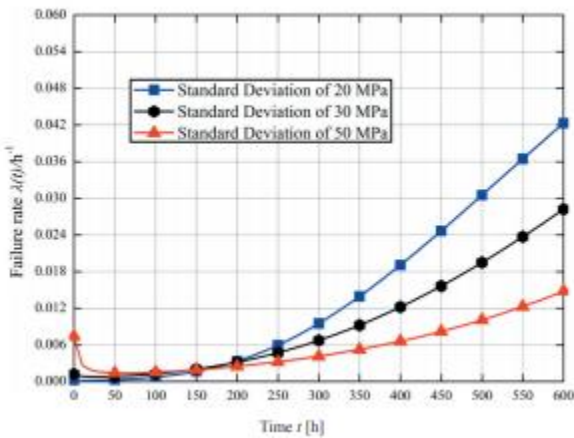
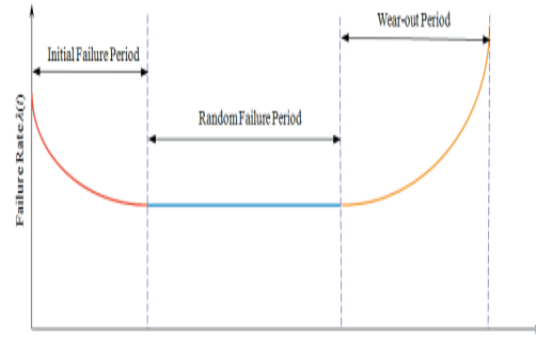


Fig. 19. Reliability of explosive bolts with different dispersions of initial strength



Material statistical characteristics have a significant impact on the dependability and failure rate of explosive bolts with varying dispersion of initial strength. As the mean starting strength rises, both dependability and failure rate go down. Furthermore, the dependability and failure rate of explosive bolts are affected by the dispersion of starting strength in diverse ways throughout the course of their lifespan. This curve is also used to depict how mechanical component failure rates change over time, as seen in Fig. 21. Item 10. Stress and initial strength measurements of explosive bolts

	$\mu(r_0)$ [MPa]	$\sigma(r_0)$ [MPa]	$\mu(s)$ [MPa]	$\sigma(s)$ [MPa]
1	400	20	300	20
2	400	30	300	20
3	400	50	300	20



The bathtub curve of mechanical components is seen in Fig. 21.

To show that our suggested model is compatible with bathtub curve theory, Figs. 18 and 20 are used to demonstrate it. Increasing the mean strength and dispersion tends to lower the random failure rate curve's slope in the random failure phase.

## CONCLUSION

The final thought and the plan for the future This study presents reliability models based on degradation of strength. The strength distribution at each load application is typically applied for examining mechanical components' dynamic dependability because it is difficult to quantitatively define the direction of strength decline. If the relationship between the residual strength at each load application in a strength degradation pathway is overlooked, reliability predictions may degrade. The recommended reliability models may be used to undertake a statistical assessment of the influence of material factors on dynamic reliability features and mechanical component failure rates. Now, it is commonly acknowledged that a broad range of initial strength does not necessarily imply a product's dependability. For mechanical components, strength deterioration may have varying implications depending on how the mechanical components' initial strength is distributed. There is a considerable association between mechanical component failure rates and a component's initial statistical characteristics. As mechanical components' mean strength and dispersion grow, the random failure rate curve's slope drops. Additional elements are being put into the dependability models in an attempt to increase their accuracy. Reliability-based design optimization is another topic of interest for the academics.

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